## Introduction and Functions

Math 131, Section 501

January 17, 2017

Math 131, Section 501

Introduction and Functions

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### Introduction

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4th year PhD student

Topological phases of matter

Functional programming

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## Motivation for the course

Critical thinking skills

Attention to detail

Mathematical maturity

Work ethic

Signalling

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## Course information

Course webpage: http://math.tamu.edu/~pgustafs/math131

Office hours: 2:00-3:00 PM Mon, 11:00-12:30 AM Thurs

Exam dates: Feb 16, Mar 23, Apr 20, May 4

Lowest exam grade

Take-home quizzes (to be worked alone, must turn them in yourself!)

## Book and Webassign

Stewart Calculus 4.0

Hard copy or ebook

Must pay for webassign

Hard copy purchase includes webassign Can just buy webassign/ebook 2 week free trial

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# Teaching Philosopy

Respect

I'm here to help you

No such thing as a stupid question

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January 17, 2017 6 / 26

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### Functions

#### Definition

A function f is a rule that assigns to each element in a set D exactly one element, called f(x) in a set E.

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## Ways to define a function

Words

A table

An algebraic rule (usual method)

A graph

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→ ∃ → January 17, 2017 8 / 26

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# Give an algebraic rule for the following function

A man runs a 10 mile race along a river bank. He runs the first x miles, then swims the rest. He runs 7 mph and swims 2 mph. Write an equation describing the time it takes him to finish the race in terms of x.

# Give an algebraic rule for the following function

An open shoe box is twice as long as it is wide and has a volume of 20 square inches. Write down the equation for the surface area of the box in terms of its width x.

## Vertical line test

#### Vertical line test

A curve in the xy-plane is the graph of a function of x if and only if no vertical line intersects the curve more than once.

#### Vertical line test examples

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12 / 26 January 17, 2017

3

# Applying functions

Let 
$$f(x) = \frac{x^2 + 1}{x + 3}$$
.

f(a)

f(2z - 1)

$$f(g(x))$$
 where  $g(x) = x^2 - 1$ 

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January 17, 2017

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13 / 26

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# Domain and range

#### Definition

The **domain** of f is the set of values x for which f(x) is defined.

#### Definition

The **range** of f is the set of all possible values f(x).

Name	Age
Alice	20
Bob	19
Charles	24
Katie	22

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## Finding the domain of a function

Rules:

- Cannot divide by 0
- Cannot take even roots of negative numbers

Cannot take logarithms of numbers  $\leq 0$ 

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## Finding the range of a function

Graph it!

$$f(x) = x^2$$

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January 17, 2017

3

16 / 26

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### Find the domain and range

$$f(x) = \sqrt{1-x^2}$$

$$f(x) = \frac{x^2(x+1)}{(x-4)^2}$$

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3

17 / 26

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### Find the domain and range

$$f(x) = x^{2/3}$$

$$f(x) = 1 - \ln(x^2 + 1)$$

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3

18 / 26

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# Even and odd functions

#### Definition

A function f is even if f(-x) = f(x) for all x.

The graph of an even function is symmetric about the y-axis.

#### Definition

A function f is **odd** if 
$$f(-x) = -f(-x)$$
 for all x.

The graph of an odd function is symmetric about the origin.

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### Is the function even, odd, or neither?

$$f(x) = x$$

$$f(x) = x^3 + 1$$

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20 / 26

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### Is the function even, odd, or neither?

$$f(x) = |x| + x^4$$

$$f(x) = \sqrt{x}$$

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January 17, 2017

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21 / 26

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## **Piecewise functions**

#### Definition

A **piecewise function** is a function that has different rules for different parts of its domain.

#### Example

$$|x| = \begin{cases} x, & x \ge 0\\ -x, & x < 0 \end{cases}$$

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## **Piecewise functions**

#### Example

$$f(x) = \begin{cases} x, & x < -1 \\ x^2, & -1 \le x < 2 \\ 4, & x \ge 2 \end{cases}$$

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23 / 26

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# Increasing and decreasing functions

#### Definition

A function f is **increasing** if f(x) increases as x increases.

A line with positive slope is increasing.

#### Definition

A function f is **decreasing** if f(x) decreases as x increases.

A line with negative slope is decreasing.

Find the intervals on which the function is increasing or decreasing.

$$f(x) = -2x + 1$$

$$f(x) = 3$$

$$f(x) = x^3$$

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January 17, 2017

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Find the intervals on which the function is increasing or decreasing.

$$f(x) = x^2$$

$$f(x) = e^{1-x}$$

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